

For the following problems you may NOT use any Matlab builtin function (unless it is explicitly stated) or language structure (such as `for`, `if`, etc.)

1. Write a one-line Matlab command that yields 1 if a 2D matrix,  $A$ , has **at least one** complex entry (i.e.  $x + yi$ ), and 0 otherwise.
2. Write an anonymous, one-line, Matlab function (`stirling = @(X)...`) that computes the Stirling's approximation for factorials. Your function must work for either a scalar or any multidimensional matrix  $X$ . If the input is a matrix, then your function must approximate the factorial of each of its elements. The Stirling's approximation to  $n!$  is given by

$$n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

where  $e = 2.71828\dots$

3. The *Pascal* matrix,  $S$ , is a  $p \times p$  square matrix containing the binomial coefficients as its elements, i.e.

$$S_{ij} = \binom{n}{r} = \frac{n!}{r!(n-r)!}$$

where  $n = i + j$  and  $r = i$ . In other words:

$$S_{ij} = {}_{i+j}C_i = \frac{(i+j)!}{(i)!(j)!}$$

where  $i$  and  $j$  are the row and column **zero-based** indexes respectively, e.g.,  $0 \leq i \leq p-1$  and  $0 \leq j \leq p-1$ .

Write a Matlab function that receives a single, scalar number  $p$ , and generates the  $p \times p$  square Pascal matrix. (*Hint: Use your `stirling` function to approximate factorials in your computation.*)